Meta-tracing makes a fast Racket

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Abstract
Tracing just-in-time (JIT) compilers record and optimize the instruction sequences they observe at runtime. With some modifications, a tracing JIT can perform well even when the executed program is itself an interpreter, an approach called meta-tracing. The advantage of meta-tracing is that it separates the concern of JIT compilation from language implementation, enabling the same JIT compiler to be used with many different languages. The RPython meta-tracing JIT compiler has enabled the efficient interpretation of several dynamic languages including Python (PyPy), Prolog, and Smalltalk. In this paper we present initial findings in applying the RPython JIT to Racket. Racket comes from the Scheme family of programming languages for which there are mature static optimizing compilers. We present the result of spending just a couple person-months implementing and tuning an implementation of Racket written in RPython. The results are promising, with a geometric mean equal to Racket’s performance and within a factor of 2 slower than Gambit and Larceny on a collection of standard Scheme benchmarks. The results on individual benchmarks vary widely. On the positive side, our interpreter is sometimes up to two to six times faster than Gambit, an order of magnitude faster than Larceny, and two orders of magnitude faster than the Racket JIT compiler when making heavy use of continuations. On the negative side, our interpreter is sometimes three times slower than Racket, nine times slower than Gambit, and five times slower than Larceny.

Categories and Subject Descriptors D.3.4 [Processors]: Code generation, Compilers; D.3.2 [Software Engineering]: Application (functional) languages

General Terms Languages, Design, Performance

Keywords Meta-tracing, JIT, Scheme, Racket, CEK

1. Introduction
Just-in-time (JIT) compilation has been applied to a wide variety of languages, with early examples including Lisp, APL, Basic, Fortran, Smalltalk, and Self (Aycock 2003). These days, JIT compilation is mainstream; it is responsible for running both server-side Java applications (Paleczny et al. 2001) and client-side JavaScript applications in web browsers (Hölttä 2013).

Mitchell (1970) observed that one could obtain an instruction sequence from an interpreter by recording its actions. The interpreter can then jump to this instruction sequence, this trace, when it returns to interpret the same part of the program. For if-then-else statements, there is a trace for only one branch. For the other branch, Mitchell suggests reinvoking the interpreter. Bala et al. (2000) applied tracing JIT compilation to optimize native assembly code and Gal et al. (2006) showed that tracing JIT compilers can efficiently execute object-oriented programs, which feature control flow that is highly dynamic and data-dependent.

Developing a just-in-time compiler is traditionally a complex undertaking. However, Bolz et al. (2009) developed meta-tracing, an approach that can significantly reduce the development cost for tracing JIT compilers. With meta-tracing, the language implementer does not have to implement a JIT compiler for their language. Instead they simply write an interpreter for their language in a special implementation language called RPython. Then some annotations (hints) can be added to their interpreter, and RPython’s tracing JIT compiler will be automatically inserted into the language implementation. Rigo and Pedroni (2006) and Bolz and Tratt (2013) describe an efficient meta-tracing implementation of Python, called PyPy.

Meta-tracing has not previously been applied to a programming language in the Scheme family. Scheme is interesting for two reasons: on the one hand, Scheme presents a number of challenges, such as continuations, guaranteed tail call optimization, heavy use of higher-order programming and multiple return values. On the other hand, Scheme has traditionally had very good ahead-of-time (AOT) compilers that do static analysis of Scheme code and optimize it heavily, such as Gambit (Feeley 2014). It is therefore an open question whether a tracing JIT compiler, and more so a non-language specific meta-tracing compiler, can compete.

In this paper we present Pycket, an implementation of the Racket language (Flatt and PLT 2010) in RPython. Pycket was written in a relatively straightforward way, closely following the control, environment, and continuation (CEK) abstract machine (Felleisen and Friedman 1987). We chose to base our interpreter on the CEK-machine for two reasons: first, the CEK-machine embodies perhaps the most straightforward way to implement a language with first-class continuations. Second, we wanted to see if meta-tracing could produce good results on an interpreter written at a higher level than the usual bytecode interpreters.

In this paper, we make the following contributions.

• We show that meta-tracing makes a CEK-based interpreter for Racket competitive with the existing AOT and JIT compilers.
• We explain the transformations we applied to Pycket to make it amenable to optimization by meta-tracing.
• We report the performance of Pycket on a standard set of Scheme benchmarks, comparing it to Larceny (Clinger and
The paper is structured as follows: in section 2 we review some of the salient features of Scheme and Racket and give some background on RPython and its tracing JIT compiler. In section 3 we describe the Pycket interpreter and the transformations that were needed to make it amenable to optimization by the RPython tracing JIT compiler. We evaluate the performance of Pycket in section 5 and discuss related work in section 6. Section 7 concludes with some future directions.

2. Background

Pycket is based on RPython and Racket; we give brief introductions to both in this section.

2.1 RPython and Meta-Tracing

RPython is a statically typed subset of Python that can be compiled into efficient C code. The types do not have to be given in the source code but are inferred. It was designed to be an implementation language for interpreters for (dynamic) languages.

The feature that makes RPython interesting is its support for meta-tracing. When compiling an interpreter written in RPython to C, optionally a tracing JIT compiler can be inserted into the generated C code. This requires some source code annotations by the interpreter author to make it work (Bolz et al. 2009, 2011b). The inserted tracing JIT compiler produces linear sequences of machine code by recording the operations the interpreter executed while running a specific piece of the user’s program. The recorded sequence of operations (called a trace) is optimized and then machine code is emitted. Traces are only produced for parts of the program that have been executed more than a specified threshold.

Because the produced machine code is linear, it needs to encode potential control flow branches in a special way. This is done with guards, an instruction that encodes the conditions that have to be true to stay on the trace. If a guard fails, execution falls back to the interpreter. If it fails often enough, a trace for that side path is produced as well. Quite often the produced traces are actually loops, meaning that they end with jumps to their own beginning.

2.2 Scheme and Racket

Scheme (Sussman and Steele Jr. 1975; Sperber et al. 2010) is a small functional language based around the imperative call-by-value λ-calculus with a core set of additional data structures. Starting with Steele (1978), Scheme also has a long history of optimizing compilers, often focusing on difficult-to-compile features such as first-class functions (in the 1970s when Scheme was invented) and first-class continuations (subsequently).

Racket (Flatt and PLT 2010) is a mature functional language and implementation, derived from Scheme with significant extensions. For our purposes, we focus mainly on areas where it overlaps with Scheme, and on its performance characteristics.

Notably for our purposes, Racket extensively uses macros and other forms of syntax extension; prior to compilation all syntax extensions are expanded into a small set of core language forms. Pycket makes use of this pass by invoking Racket itself to perform this expansion, and then implements only the dozen core forms.

The current Racket implementation features both an AOT compiler and a JIT compiler. The AOT compiler takes the core forms mentioned above and produces a stack-based bytecode. At runtime, upon first invocation of a function, the bytecode of the function is compiled to machine instructions by the JIT compiler.

The implementation strategy of Racket places most optimization burden on the AOT compiler to bytecode. This compiler performs a number of transformations important for functional languages such as lambda-lifting, as well as standard transformations such as constant propagation and dead code elimination. In particular, significant inlining is performed in this pass, including inlining of recursive functions, resulting in a kind of loop unrolling.

Because the Racket JIT compiler is invoked on the first call to a function, it can only take advantage of dynamic information present at that time. Therefore, while the JIT compiler does make use of information such as types of constant references, it does not perform the kind of dynamic optimizations often associated with JIT compilers for dynamic languages. In particular, it does not feed back type information collected at runtime about variables into the compiler (Hölzle and Ungar 1994).

3. The Implementation of Pycket

Pycket is implemented directly as an interpreter for the CEK abstract machine (Felleisen and Friedman 1987), with only minor modifications. The CEK-machine is a well-known abstract machine that makes environments and continuations explicit in the representation and it represents control using abstract syntax trees (ASTs).

States within the CEK-machine are triples of an expression to be evaluated, the environment of that expression which stores bindings of names to values, and a continuation object that describes what to do after the expression has been evaluated. The machine is a set of rules describing transitions between these states. We implement mutation using the Python heap, instead of an explicit heap as in the CESK-machine.

Following the CEK-machine has a number of advantages. First, it makes supporting difficult-to-implement Racket features such as call/cc, proper tail calls, and multiple return values straightforward. Second, using the CEK-machine as a starting point is also interesting in that, implemented naively, it is not a particularly efficient way to execute Scheme-like languages. It is therefore an excellent way to test the hypothesis that RPython’s meta-tracing can generate an efficient implementation from such a high-level interpreter. 1

Listing 1 shows the main loop of the Pycket interpreter. The local variables represent the current expression to be evaluated (ast), the current environment (env), and the continuation (cont). In every iteration of the loop, one transition rule of the CEK-machine is applied, by calling the method interpret on the current ast (line 4), which returns a new triple ast, env, cont. For transitions that produce values, the interpret method decides what to do next by invoking the plug.reduce method on the current continuation cont. If the computation is finished, a special done exception is thrown, which encapsulates the return value.

The main loop has two hints to RPython’s JIT compiler generation machinery, on lines 3 and 5–6. These hints are discussed further in section 4, but they do not affect the semantics of the program.

```python
try:
  while True:
    jitdriver.jit_merge_point()
    ast, env, cont = ast.interpret(env, cont)
    if ast.should_enter:
      jitdriver.can_enter_jit()
    except Done, e:
      return e.values
```

Listing 1. Interpreter main loop

1 While a direct interpreter on the AST would be even more high-level, it would make it harder to implement continuations, and would require proper tail calls from the underlying language, which RPython does not provide.
3.1 Expressions

The AST is a representation of the program being interpreted. The
AST has to represent only the core forms, with the remainder
handled by Racket’s macro expander; these forms are lambda ab-
stractions, function application, quotes, variables, let bindings, if,
letrec, begin, and set! As an example, the AST class representing
if-expressions is seen in listing 2.

An if-expression references a test, a then-expression and else-
expressions, all of which are themselves ASTs. To interpret an if-
expression, first the test is evaluated and the value resulting from
that evaluation is compared to #f. Depending on whether that is
true or false, the then- or the else-expression is returned as the new
AST to be interpreted. The environment and continuation remain
the same.

```python
class If(AST):
    # constructor omitted
    def interpret(self, env, cont):
        val = self.tst.interpret(env)
        if val == values.false:
            return self.els, env, cont
        else:
            return self.thn, env, cont
```

Listing 2. If AST node

3.2 Continuations

Continuations encapsulate what the interpreter must do after the
current AST is fully evaluated to a value. We represent continuations
as a stack implemented as a linked list. The chain of continuations
combines the roles of an operand stack and the procedure call stack
of a more traditional bytecode interpreter.

As a simple example, listing 3 shows the begin continuation,
implementing the begin form. This form evaluates a sequence of
expressions, returning the value of the last. The begin continuation
is therefore used to mark that the results of all but the last expression
are ignored. The plug_reduce method of a continuation is called with
the result of evaluating the previous expression in the begin
form as the vals argument. That value is then ignored and the next
expression is evaluated. For the last expression of the begin no new
continuation is needed, and the value of that expression is eventually
passed on to the previous continuation.

```python
class BeginCont(Cont):
    # constructor omitted
    def plug_reduce(self, vals):
        jit.promote(self.ast)
        for i, s in enumerate(self.env_structure.symbols):
            if s is sym:
                v = self.value_list[i]
                assert v is not None
                return v
        return self.prev.lookup(sym, env_structure.prev)
```

Listing 3. Begin continuation

As an optimization, we fuse the expression re-construction (plug)
and new-expression evaluation (reduce) portions of the CEK-
machine, a standard practice in optimizing abstract machines. Thus
the plug_reduce method directly finds the next expression to evalu-
ate.

Prior to interpretation, we translate all expressions to A-normal
form (Danvy 1991; Flanagan et al. 1993). This introduces additional
let-bindings for all non-trivial expressions (e.g. function application),
so that function operands and the test of an if are always ei-
ther constants or variables. This transformation is not required for
our implementation, but significantly simplifies the continuations
we generate, enabling the tracing JIT compiler to produce better
code.

3.3 Environments

Environments are implemented as linked lists of arrays of values.
Listing 4 shows the implementation of the environment class. It
stores a list of values and a reference to the outer environment. AST
nodes track the lexical nesting structure, meaning that environments
need not store variable names (see section 4.2).

Almost all variables in typical Racket programs are immutable, but
set! must also be supported. To simplify the representation
of environments, Pycket performs assignment conversion: every
mutable variable is transformed into an immutable one whose value
is a mutable heap cell. This makes mutable variables somewhat
slower, but benefits all others by enabling the JIT compiler to look
up variables only once.

```python
class ConsEnv(Env):
    # constructor omitted
    def lookup(self, sym, env_structure):
        jit.promote(env_structure)
        for i, s in enumerate(env_structure.symbols):
            if s is sym:
                v = self.value_list[i]
                assert v is not None
                return v
        return self.prev.lookup(sym, env_structure.prev)
```

Listing 4. Environment and lookup

Pycket also simplifies environment and closures to handle simple
recursive functions, as is common in functional language imple-
mentations. For example Pycket implements a simplified form of
the letrec rewriting for procedures (Waddell et al. 2005).

3.4 Values

Values in Racket are represented straightforwardly as instances of
several classes, one class for each kind such as fixnum, flonum,
bool, pair, vector, etc. We specialize the representation of vectors
to enable unboxed storage for homogeneous vectors of fixnums or
flonums using the storage strategies technique (Bolz et al. 2013).

Racket’s pairs are immutable (mutable pairs are constructed by
cons and accessed with car and cdr). Therefore it is possible to
choose one of several specialized representations of pairs at
allocation time. Currently Pycket only specializes pairs when the
car is a fixnum, which it represents in unboxed form.

In all other cases, unlike Racket and almost all other functional
language implementations, fixnums are heap allocated. Pycket does
not use pointer tagging.

4. Interaction with Meta-Tracing

One immediate hurdle when applying RPython’s meta-tracing JIT
compiler to Pycket is that one of the hints that the interpreter au-
thor needs to give is where loops at the language level can occur.
Because Racket transforms loops into recursive function calls, we
mark the start of a function as a place where the JIT compiler should
start tracing. This is done by setting a flag should_enter on the body
AST of every lambda form. The bytecode dispatch loop (listing 1)
reads the flag (line 5) and calls the corresponding method on the
JIT driver (line 6). Another hint is given just inside the loop body,
indicating that this is the main loop of the interpreter (line 3).
A further set of hints indicate that data structure are immutable. RPython assumes that all instances are mutable; since ASTs, continuations, and environments are immutable, they can be marked as such. Finally, many functions in the interpreter contain loops which should be unrolled while tracing, specified by a function decorator (listing 4, line 3).

A small further optimization is the creation of size-specialized classes for many classes in the interpreter, such as ConsEnv and continuation frame classes. This removes a layer of indirection by putting the content directly into the class.

4.1 Allocation-Removal

The main optimization that the JIT compiler performs after it has traced a hot piece of code is that it removes allocations of immediate data structures that have a predictable lifetime (Bolz et al. 2011a). This optimization is particularly important for Pycket. When running the interpreter without meta-tracing, a lot of data-structures are continually allocated: every call to an interpret method allocates a new triple as its return value and new continuations are instantiated all the time. Most of the time these do not live very long, and the JIT compiler can fully remove the overhead of their use. In particular, simple tail-recursive functions are turned into loops on the machine code level that, most of the time, do not need to allocate environments or continuations.

For recursive functions where the recursive call is not in tail position the situation is slightly more interesting. The JIT compiler still produces a loop from the start of the function to the recursive call. However, because there is something left to do after the base case is reached, every iteration of the loop allocates a continuation. This continuation records what is left to do upon the return of the recursive call. When the base case is eventually reached, these continuations are then activated and removed again. This produces a second loop which effectively unwinds the stack of continuations. In this way, even recursion that cannot be directly mapped to iteration is compiled as two loops in Pycket.

4.2 Lexical Addressing for Free

During the rewriting of the AST, another piece of information is computed for every AST node. Since Racket is lexically scoped, it is possible to determine the static structure of the environment at every point in the AST. Environments are linked lists of arrays of values, thus static environments are a linked list of lists of names. In traditional Scheme systems this environment structure is used to assign two numbers to every variable which encode the position of the variable in the stack of frames. In Pycket, this encoding is not necessary. Instead, every time a variable in the environment is examined, the structure of the environment is traversed in parallel to the environment, until the looked-for name is found. While this appears much less efficient than just using the two indices to pick the right place, the JIT compiler will produce the same machine code as if the encoding to numbers was used.

This works because the environment structure is an immutable data structure that is part of the AST. Thus, the JIT can constant-fold all computations that inspect it. In particular, in listing 4, the loop on line 6 is unrolled and the condition on line 7 is constant-folded. The generated code simply traverses the stack of environments to the right one, and then reads the value at the correct index.

The approach is made possible by separating the static part of the environment, its structure, from the data structure that stores different values at runtime. The technique of separating static and dynamic data structure components is common in the context of partial evaluation, and called binding time improvement (Jones et al. 1993, Chapter 12). Jørgensen (1992) provides an example of using binding time improvement for environments.

Table 1. Extreme runtimes in milliseconds

<table>
<thead>
<tr>
<th></th>
<th>Gambling</th>
<th>Larceny</th>
<th>Pycket</th>
<th>Racket</th>
</tr>
</thead>
<tbody>
<tr>
<td>ctak</td>
<td>859±36</td>
<td>1965±15</td>
<td>304±1</td>
<td>40774±81</td>
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<tr>
<td>fibc</td>
<td>768±52</td>
<td>1750±28</td>
<td>1061±2</td>
<td>27064±94</td>
</tr>
<tr>
<td>pi</td>
<td>657±7</td>
<td>44742±234</td>
<td>624±4</td>
<td>502±2</td>
</tr>
</tbody>
</table>

5. Results

We compared Pycket to Racket and several Scheme implementations to test its performance and therefore our hypothesis.

Hardware We conducted the experiments on an Intel Xeon E5410 (Harpertown) clocked at 2.33 GHz with 2x6 MB cache and 16 GB of RAM. All benchmarks used are single-threaded, hence the number of cores (four) was irrelevant to the experiment. Although virtualized on Xen, the machine was dedicated to the benchmarks.

Software The machine ran Ubuntu 12.04.4 LTS with a 64 bit Linux 3.2.0. We used the benchmarking framework ReBench\(^2\) to carry out all executions and measurements. RPython as of revision 8d6c4a658f30 served for translating Pycket.

Implementations Racket v6.0, Gambit v4.7.2, Larceny v0.97, and Pycket as of revision 10ed5db6a395 were used in the benchmarks. All Gambit programs were compiled with -D__SINGLE_HOST.

Benchmarks The benchmark suite consists of the “CrossPlatform” benchmark from Larceny, comprising well-known Scheme implementations originally collected for Gambit. We omit those benchmarks that use mutable pairs, as well as those using I/O and threads, which we have not yet implemented.

Methodology Every benchmark was run 10 times uninterrupted at highest priority, in a new process. The runtime (total time) was measured in-system and, hence, does not include start-up; however, warm-up was not separated, so JIT compiler runtime is included in the numbers. We report the arithmetic mean of the ten runs along with bootstrapped (Davison and Hinkley 1997) confidence intervals showing the 95% confidence level.

The results are summarized in Figure 1. The runtime per benchmark of each implementation is normalized to Racket. Pycket’s performance on individual benchmarks ranges from approximately three times slower to two times faster than Racket, in nine instances even faster than Gambit. The geometric mean of all measurements compared suggests that Pycket is about as fast as Racket, as depicted by the bars labeled “geometric mean” in the figure.

Three benchmarks are not included in the comparison above, as the differences were so extreme that they skew the overall numbers. As Table 1 suggests, Pycket was one to two orders of magnitude faster than Racket for the ctak and fibc benchmarks. Both make heavy use of continuations, and hence benefit from the CEK-machine nature of Pycket, whereas Racket’s implementation of continuations is known to be slow. On these benchmarks, Pycket is close to or faster than Gambit and Larceny. On the pi benchmark, which emphasizes bignum performance, Larceny is much slower than the other implementations.

Pycket with the meta-tracing JIT compiler disabled runs generally 40 times slower than the meta-traced version.

6. Related Work

As mentioned in the introduction, functional languages in general, and Scheme in particular, have a long tradition of highly optimizing AOT compilers. Rabbit, by Steele (1978), following on the initial design of the language, demonstrated the possibilities of continuation-passing style and of fast first-class functions. Subsequent systems such as Gambit (Feeley 2014), Bigloo (Serrano and Weis 1995), Larceny (Clinger and Hansen 1994), Stalin (Siskind 1992), and others provide examples.

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\(^2\)https://github.com/smarr/ReBench
1999), and Chez (Dybvig 2011) have pioneered a variety of techniques for static analysis, optimization, and memory management, among others. Most other Scheme implementations are interpreters, either directly on the AST or on a bytecode representation. Racket is the only widely used system in the Scheme family with a JIT compiler, and even that is less dynamic than many modern JIT compilers.

Many Lisp implementations provide means for programmers to manually type-specialize code with specialized operations or type declarations. Racket provides these operations, but we have not yet evaluated their effect on performance in Pycket.

JIT compilation has been extensively studied in the context of object-oriented, dynamically-typed languages (Aycock 2003). For Smalltalk-80, Deutsch and Schiffman (1984) developed a JIT compiler from bytecode to native code. Chambers et al. (1989) explored using type specialization and other optimizations in Self, a closely-related language. Further research on Self applied more aggressive type specialization (Chambers and Ungar 1991) and improved the compiler’s selection of methods (Hölzle and Ungar 1994).

With the rise in popularity of Java, JIT compilation became a mainstream enterprise, with a significant increase in the volume of research. The Hotspot compiler (Paleczny et al. 2001) is representative of the Java JIT compilers. JIT compilation has also become an important topic in the implementation of JavaScript (see for example (Hölttä 2013)) and thus a core part of modern web browsers. For strict functional languages other than Scheme, such as OCaml, JIT compilers exist (Starynkevitch 2004; Meurer 2010), however, they are typically auxiliary to the usually much faster AOT compiler implementations.

As mentioned in the introduction, Mitchell (1970) introduced the notion of tracing JIT compilation, and Gal et al. (2006) used tracing in a Java JIT compiler. Since then, Gal et al. (2009) developed a tracing JIT compiler for JavaScript and LuaJIT\(^3\) is a very successful tracing JIT compiler for Lua. Further work was done by Bebenita et al. (2010) who created a tracing JIT compiler for Microsoft’s Common Intermediate Language (CIL) and applied it to a JavaScript implementation in C#: Schilling (2013, 2012) developed a tracing JIT compiler for Haskell based on LuaJIT called Lambda
dichine. Due to Haskell’s lazy evaluation, the focus is quite different than ours. One goal of Lambdachine is to achieve deforestation (Wadler 1988; Gill et al. 1993) by applying allocation-removal techniques to traces. Lambdachine is between 50% faster and two times slower than GHC on the small benchmarks the thesis reports on (Schilling 2013).

The core idea of meta-tracing, which is to trace an interpreter running a program rather than a program itself, was pioneered by Sullivan et al. (2003) in DynamoRIO.

There were experiments with applying meta-tracing to a Haskell interpreter written in RPython (Thomassen 2013). The interpreter also follows a variant of a high-level semantics of the Core of Haskell (Launchbury 1993). While the first results were promising, it supports a very small subset of primitives so that not many interesting benchmarks run on it.

7. Future Directions

With approximately two person-months of effort, Pycket has demonstrated that meta-tracing JIT compilers are competitive with mature AOT compilers for classic functional programming languages. RPython’s meta-tracing approach takes a simple implementation of the CEK-machine and turns it into fast machine code.

However, much remains to investigate in this direction. As we have seen, Pycket is on-average almost two times slower than Gambit, and significantly slower than that on some benchmarks. We conjecture that this gap can be closed, but more work is required to find out. Additionally, Pycket does not yet implement some of Racket’s runtime features, including threads, continuation marks, and delimited control operators. These features may require changes that significantly affect performance, but we conjecture that they do not since they map naturally onto our CEK-machine architecture.

Additionally, a wide variety of further optimization opportunities present themselves. For example, while we implement storage strategies for vectors, all integers stored in environment locations, heap cells, and continuations are boxed—storage strategies may also have a role to play here. They may also allow us to implement Racket’s ubiquitous lists in new ways, taking advantage of new functional data structures such as Hash-Array Mapped Tries (Bagnell 2001). We plan to investigate whether tracing provides performance advantages for complex control flow such as that generated by contract checking, objects implemented via macros and structures, or even interpreters written in Racket itself. Finally, since meta-tracing has accelerated the CEK-machine so effectively, these techniques may also apply to other abstract machines.

\(^3\)http://luajit.org

![Figure 1. Benchmark runtime results. Each bar shows the arithmetic mean of 10 runs, normalized to Racket.](image-url)
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References


## Table 2. All benchmarks

<table>
<thead>
<tr>
<th>Benchmark</th>
<th>Gambit</th>
<th>Larceny</th>
<th>Pycket</th>
<th>PycketNoJit</th>
<th>Racket</th>
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<td>2861 ms ± 25</td>
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<td>2930 ms ± 18</td>
<td>97819 ms ± 1504</td>
<td>3104 ms ± 33</td>
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<td>earley</td>
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<td>848 ms ± 5</td>
<td>265 ms ± 2</td>
<td>54706 ms ± 276</td>
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<tr>
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<td>3714 ms ± 27</td>
<td>117401 ms ± 2132</td>
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<td>17831 ms ± 46</td>
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<td>3511 ms ± 34</td>
<td>27192 ms ± 76</td>
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<tr>
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<td>62351 ms ± 385</td>
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<td>1594 ms ± 26</td>
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<td>87984 ms ± 677</td>
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<td>1956 ms ± 11</td>
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<td>519 ms ± 1</td>
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